

Radar Waveform Design For High Resolution Doppler Target Detection

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Abstract: This paper addresses the problem of optimum waveform design for multiple target detection. The notion of poly-semantic radar, which gave improved performance through coincidence detection, is analyzed for high resolution radar system in presence of high density additive noise and Doppler shift. These sequences are optimized by employing Hamming backtrack algorithm (HBT). The detection capability of poly-semantic sequences is further improved through coincidence detection of the return signal. The simulation results show that the proposed sequences give improved robustness of noise and Doppler shift for HRR target detection compared to conventional pulse compression sequences.

Keywords: Hamming backtrack algorithm, high resolution radar, target detection.

I. Introduction

In high resolution radar (HRR) systems, there is a need to employ sequences of larger lengths to achieve high pulse compression ratios [1], [2]. The Optimal binary codes (OBC) including Barker code (B13) and Golay codes [3] provide significant advantages in terms of detection and sidelobe suppression [4], but these codes are available at lower lengths less than 60. Earlier the generation of optimal sequences at higher length up to 5000 is developed for poly-alphabetic and bi-alphabetic sequences [5]-[7]. In poly-alphabetic radar [5] what is transmitted is a specially designed binary sequence so that there is no change in the transmission technology. On reception, it is decoded before further processing. This is a change in the current practice, the resistance to which has weakened, as decoding before further processing is also required by neural network processing [8]-[10] of radar return signal for additional advantage. After decoding, the return signal is subjected to multiple interpretations. Here, a binary sequence is transmitted, but through poly-gram reading, it can also be interpreted as quaternary and octal sequences. Thus, it is as if one sequence is physically transmitted, but three sequences are notionally transmitted and received. They can therefore be processed separately at the receiver to set up coincidence detection. In poly-alphabetic sequence design a bigram viewed as a quaternary element or a trigram viewed as an octal element is some what of a constrained concept. The Quaternary and octal elements as independent entities would have 3 and 7 first order Hamming neighbors, but bigrams and trigrams on the substratum of binary monograms, which undergo Hamming scan have only two and three first order Hamming neighbors. Thus, the higher order poly-gram interpretations have a disadvantage in Hamming scan. Also, the enlarged alphabets deteriorate the noise and Doppler robustness at higher lengths in poly-alphabetic sequence [6].

In order to overcome these drawbacks and to restrict the enlarged alphabets of poly-alphabetic sequence to binary, the poly-semantic sequences are proposed [11]. These sequences are mono-alphabetic nature of poly-alphabetic sequences. The work presented in [11] did not discuss about noise rejection ability of these sequences for detection a target in noise environment conditions. The work presented in this paper is an attempt to evaluate the detection ability of mono-alphabetic poly-semantic sequences for the application to high resolution radar in presence of high dense noise and Doppler frequency. In this paper, the detection performance of the detected signal in presence of additive noise and Doppler shift is evaluated in terms of figure of merit.

The figure of merit is defined [12] as,

$$F^{(m)} = \frac{\overline{C^{(m)}(0)} - \max_{k \neq 0} [C^{(m)}(k)]}{C^{(m)}(0)} \quad (1)$$

Here 'm' represents the number of bit errors obtained in the sequence. Thus, the figure of merit in (1) is defined in the context, when known number decoding errors are present in the detected signal. It is assume that distortion due to propagation delay is ignored. Also, the additive noise is independent with transmitted signal. But, in real time situation, the received signal is corrupted by random noise with unknown noise

strength. If the additive noise exceeds the threshold level (at the detector), the received sequence is not true replica of transmitted signal. The resulting signal at the output of the detector will undergo any number of bit errors. Then the optimal waveform design problem is solved by redefining the measure of performance in (1) by taking into the effect of additive random noise at given signal to noise ratio (η) as discussed in Sec. II.

II. Design Algorithm And Associated Concepts

The concept of mono-alphabetic poly-semanticism [11] is similar to adaptation of the self-cooperative sequences. A binary sequence S with good autocorrelation properties is designed. It is doubled in length by interleaving another binary sequence T_1 whose elements are so chosen that enlarged sequence is good. Yet another sequence T_2 is interleaved to triple the length and the elements of former are so chosen that the new enlarged T_3 sequence has good autocorrelation.

$$\text{Let, } S = [S_0, S_1, S_2, \dots, S_{N-1}] \tag{2}$$

Be a transmitted signal of length N ,

$$R = [R_0, R_1, R_2, \dots, R_{N-1}] \tag{3}$$

Is received signal. Here, $R = S + W$; where W is the additive noise signal at given η .

Now, (1) is redefined as

$$F_\eta = \frac{\overline{C_\eta(0)} - \max_{k \neq 0} [C_\eta(k)]}{\overline{C_\eta(0)}} \tag{4}$$

Where, F_η is the figures of merit at given η .

The cross correlation between S & R at given η is

$$c_\eta(k) = \sum_{i=0}^{N-1-k} s_i r_{i+k}, \quad k = 0, 1, 2, \dots, N-1 \tag{5}$$

$$\text{Also, } F_\eta = 1 - \frac{\max_{k \neq 0} [C_\eta(k)]}{\overline{C_\eta(0)}} \quad \text{or} \quad F_\eta = 1 - \frac{1}{D_\eta} \tag{6}$$

$$\text{Where, } D_\eta = \frac{\overline{C_\eta(0)}}{\max_{k \neq 0} [C_\eta(k)]} \tag{7}$$

Is the discrimination at given η .

The over head bars in (4) & (6) denote the averaging over the ensemble of R . The work presented in this paper considers the ensemble of R with 100 runs of additive noise signals in order to obtain more accurate performance. Here, F_η is a monotone function of D_η as in (6). When D_η goes to infinity, F_η becomes unity.

The range of F_η is from 0 to 1, making F_η a non-euphuistic measure.

In the detection process by employing coincidence detection, the return signal R is triply processed to exploit the goodness at three different stages of construction. The criterion of goodness, which is used for design, takes into account the interaction of the three interleaved sequences T_1, T_2 , and T_3 .

Hamming Backtrack Algorithm For PSS

To optimize the performance of goodness, the poly-semantic sequences should undergo Hamming scan [5] by considering figure of merit as desideratum. The Hamming scan algorithm may not perform recursive search among all these Hamming neighbors and results in suboptimal solution to the signal design problem. When poly-semantic Hamming scan yields no sequence with a figure of merit better than the previous sequence, the backtracking Hamming scan algorithm can be employed to improve further the objective function of the resulting sequence. It considers a prescribed number n called span of the best Hamming neighbors (though they are all inferior to starting sequence) and improves them separately by repeated recursive Hamming scan, say c times (called climb). If some sequences superior to the starting poly-semantic sequence results, the best among them is selected. A span of 6 and a climb of 2 is used in the proposed

algorithm. If the Hamming backtracking succeeds in improving the value of figure of merit, the search can resume by further application of poly-semantic Hamming scan.

Phase Reversal Effect Due To Doppler Shift

Another advantage of poly-semantic sequence arises because of its bi-phase mono-alphabetic nature. The bit error due to Doppler frequency occurs when the phase shift of the pulse exceeds $\pm\pi/2$ unlike the poly phase sequence which results into a bit error when phase shift exceeds $\pm\pi/M$, where M indicates the number of phase levels in the sequence. Fig. 1(a) shows the range of phase shift without bit errors for bi-phase sequences (M=2) and Fig. 1(b) for poly-phase sequences with M = 4.

In noise free environments, the phase shift added due to Doppler to the sub-pulses is monotonic function as required for goodness of measure. In poly-semantic sequences of length N, the maximum phase shift allowed on each sub-pulse of duration $\tau = T/N$ sec without bit errors is less than $\pm\pi/2N$. Where as in poly-phase sequences the maximum allowable phase shift is less than $\pm\pi/MN$ without bit errors. Therefore the poly-semantic sequences have M/2 times more Doppler tolerance when compared to poly-phase sequences.

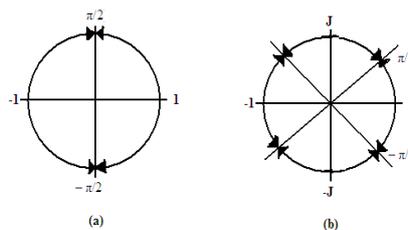


Fig. 1 Range Of Phase Shift without Bit Errors (A) For Bi-Phase Sequences (M=2) (B) Poly-Phase Sequences With M = 4.

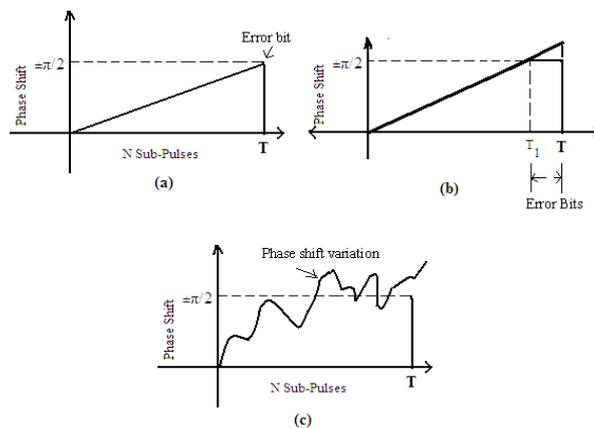


Fig. 2 Doppler Phase Shift On Received Bi-Phase Sequences (A) When Phase Shift Is Equal To $\pm\pi/2$ (B) When Phase Shift Is Greater Than $\pm\pi/2$ (C) When Additive Noise Is Added Along With Doppler Phase Shift.

In poly-semantic sequences, when the phase shift is equal to $\pm\pi/2$, the last sub-pulse in the sequence takes phase reversal. So the last bit produces an error as shown in Fig. 2 (a). When the phase shift exceeds $\pm\pi/2$, the bits within the period T_1 & T (where, $T_1 < T$) in Fig. 2(b) results into an error.

III. Poly-Semantic Radar Signal Processor

The generation of poly-semantic sequences is completed in two steps: first one using restricted (selective) Hamming backtracking scan for interspersed binary sequences and the second, using a complete Hamming backtracking scan with an appropriate joint objective function, which takes into the account of correlation properties between the received sequence R and predefined interleaved sequences in the process of signal design. The block schematic diagram of poly-semantic radar signal processor at the transmitter is shown in Fig. 3

First Step In The Signal Design

Consider, optimal binary codes or randomly generated binary codes of length N, given by

$$S_1=A=[a_j] \tag{8}$$

$$B=[b_j] \tag{9}$$

And $C=[c_j] \tag{10}$

Where, $j = 0, 1, 2, 3, \dots, N-1$.

The elements of these sequences are drawn from alphabet $\{-1, +1\}$.

The sequence S_1 is mutated viz. $+ \rightarrow -, - \rightarrow +$ using Hamming backtracking scan algorithm to get optimum figure of merit. The sequences S_2 of length $2N$ and S_3 of length $3N$ are generated by interleaving the elements of S_1 & B and S_2 & C respectively as shown in Fig. 3(a). Therefore

$$S_2=[a_j b_j] \tag{11}$$

And $S_3=[a_j b_j c_j] \tag{12}$

Where, $j= 0, 1, 2, 3, \dots, N-1$.

A selective Hamming backtracking scan algorithm [10] is applied on the sequences S_2 and S_3 , so that the figure of merit of the output sequence is optimized. This algorithm performs mutations only on the embedded elements, i.e., $b_0, b_1, b_2, b_3 \dots$ of the sequence S_2 , and $c_0, c_1, c_2, c_3 \dots$ of the sequence S_3 , without disturbing the other elements.

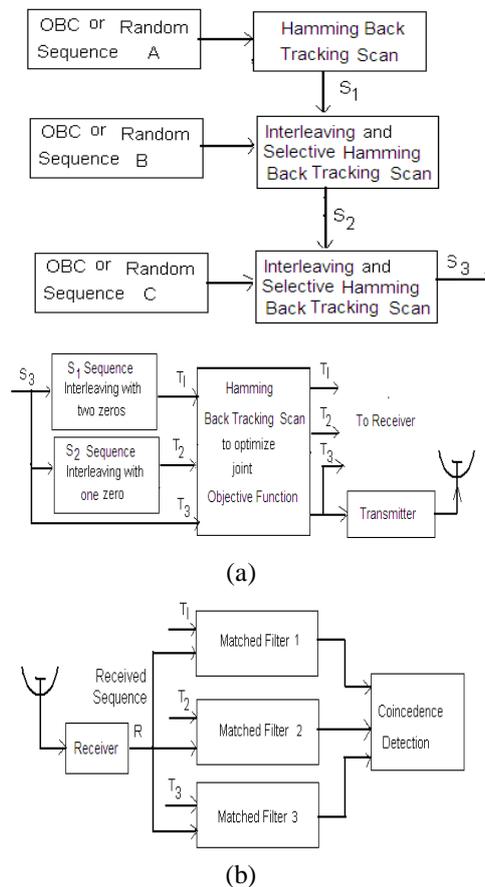


Fig. 3 Block Schematic Diagram of Poly-Semantic Radar Signal Processor (A) Transmitter (B) Receiver.

Second Step In The Signal Design

The sequence S_3 is interspersed by binary sequences S_1 and S_2 . It is equivalent to three sequences with good autocorrelation properties being transmitted in the form of S_3 . On reception, the received waveform is decoded into binary sequence (R) and the cross correlation is computed in discrete mode. The decoded sequence R is cross correlated in the receiver with three pre designed sequences, given by

$$T_1 = [a_0, 0, 0, a_1, 0, 0, a_2, 0, 0 \dots a_{n-1}, 0, 0] \tag{13}$$

$$T_2 = [a_0, b_0, 0, a_1, b_1, 0, a_2, b_2, 0 \dots a_{n-1}, b_{n-1}, 0] \tag{14}$$

$$T_3 = [a_0, b_0, c_0, a_1, b_1, c_1, a_2, \dots a_{n-1}, b_{n-1}, c_{n-1}] \tag{15}$$

The Hamming scan algorithm is applied on T_1 , T_2 , and T_3 for optimizing the joint figure of merit $F = (F_1+F_2+F_3) / 3$. Here, F_1 , F_2 , and F_3 are obtained by cross correlation of the sequences S_3 & T_1 , S_3 & T_2 , and S_3 & T_3 respectively. The good figure of merit properties of these three interpretations are jointly used through coincidence detection for the detection of target. The binary sequence $S_3(T_3)$ is transmitted as a waveform.

The signal processing system at the receiver is shown in Fig. 3(b). On reception, the received waveform which is perturbed by Gaussian noise and / or Doppler shift is decoded into binary sequence (R). The received binary sequence R is cross correlated with three embedded sequences T_1 , T_2 , and T_3 (or S_3) in three channels separately. The three cross correlation peaks in three channels coincide, which simultaneously indicates the presence of the target (Fig. 9). It can also be observed that the time sidelobes in three channels do not align. This in turn reduces the degree of false alarm because of time sidelobes in the return signal.

IV Simulation Results and Performance Evaluation

Noise Robustness

When the PSS is perturbed by additive noise of different strengths, the noise effect on figures of merit at different sequence lengths is shown in Fig. 4. The noise performance is examined for different values of η ranging between 0 db to -20 db. The noise performance results clearly show that the PSS exhibits high noise robustness at the higher sequence lengths.

Doppler Tolerance

As explained in Sec. II, when the target has a constant motion, a linear phase shift given by $d\phi = \sigma\pi / N$, $0 < \sigma \leq 1$ proportional to target velocity will be added on to the received decoded sequence. The performance of poly-semantic sequences in terms of figure of merit without additive noise is shown in the Fig. 5 at different Doppler phase shifts (ϕ_d) in the interval of $[0.4\pi/N, 0.8\pi/N]$ per sub-pulse. It is observed from the figure that as Doppler shift increases above $0.5\pi/N$, the performance of figure of merit deteriorates.

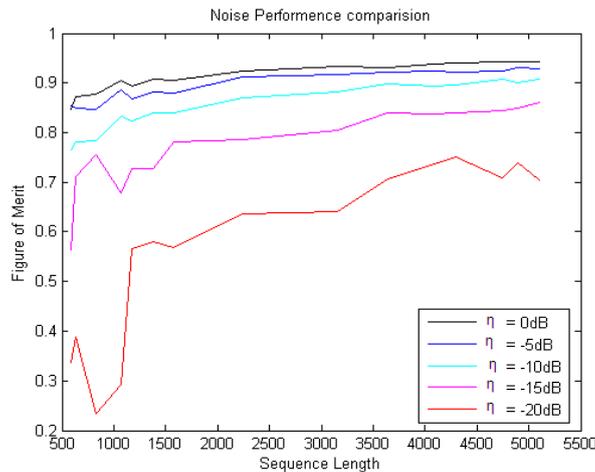


Fig. 4 Noise Performance of Poly-Semantic Sequences

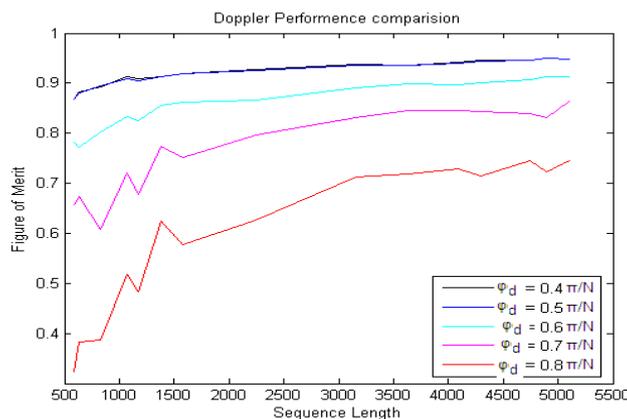


Fig. 5 Doppler Performance of Poly-Semantic Sequences

When Doppler phase shift increases to $0.8\pi/N$, the figure of merit falls below 0.3 (Fig. 5). Thus the information due to target will be masked and it is not possible to identify the target. The proposed sequences have Doppler tolerance up to $0.7\pi/N$ with corresponding figure of merit of 0.3.

Combined Effect of Noise and Doppler Shift

When the signal encounters the joint effect of additive noise and Doppler shift due to a moving target, the phase shift variation in the received signal becomes non-monotonic function as shown in Fig. 2(c). In such a case some of the sub-pulses (randomly) in the sequences may have phase shift more than $0.5\pi/N$. At threshold detection these sub-pulses undergo phase reversal. The performance of figure of merit decreases with the increase of such erroneous bits in the decoded sequence. This results into deterioration in the performance of PSS detection. Fig. 6 gives the figure of merit of PSS sequences at different lengths $N=500$ to 5000 at $\eta = 0$ dB and varying Doppler shift in the interval $[0.4\pi/N, 0.8\pi/N]$.

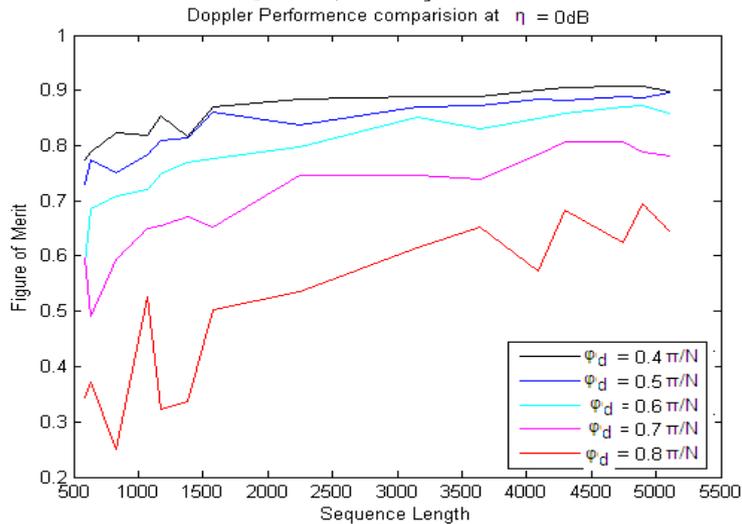


Fig. 6 Noise and Doppler Performance of Poly-Semantic Sequences at Different Doppler Phase Shifts (Φ_d) and Fixed η of 0 dB.

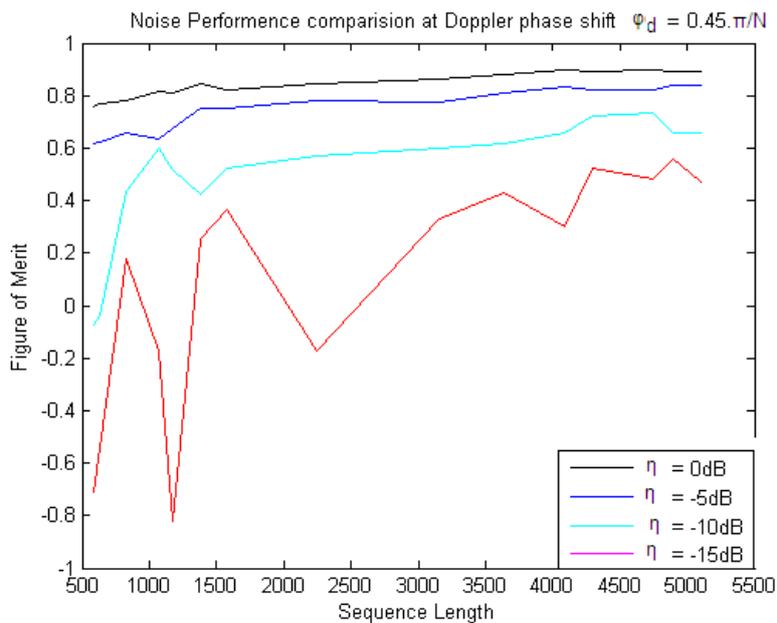


Fig. 7 Noise and Doppler Performance of Poly Semantic Sequences at Different Noise Levels of η and Fixed Doppler Phase Shift of $0.45\pi/N$.

Also, Fig. 7 shows at fixed Doppler shift of $0.45\pi/N$ and varying η . It is observed that the sequences exhibits more Doppler tolerance at higher length when compared to lower length since the phase variation per bit is small at higher lengths.

Range Resolution

Here, we have considered only two point targets, which are moving with same velocity within the resolution volume. The following target model is developed with Doppler shift in noisy environment. This model is simulated using MATLAB functions. Two targets, which are separated from different sub-pulses delay apart (SPDA) with sub-pulse duration ‘ τ ’ of 50 ns (range resolution 7.5 m) are considered. In principle, the same procedure can be extended to obtain range resolution for multiple targets, which are separated from one SPDA to (N-1) SPDA. When targets are within the sub-pulse range, the resultant echo signal is the addition of all the echo signals from the targets. Depending on the delay between the echo signals, the length of the resultant sequence increases. Fig. 8 is designed as a simulated target model for generating received code S_R , when two targets are at n- SPDA ($n = 0, 1, 2, \dots, N-1$) with Doppler shift f_d in noisy environment. The binary code S_b is clocked (2N-1) times into the target model to get the received code S_R of fixed length (2N-1). Limiter is used to limit the amplitude levels between ± 1 .

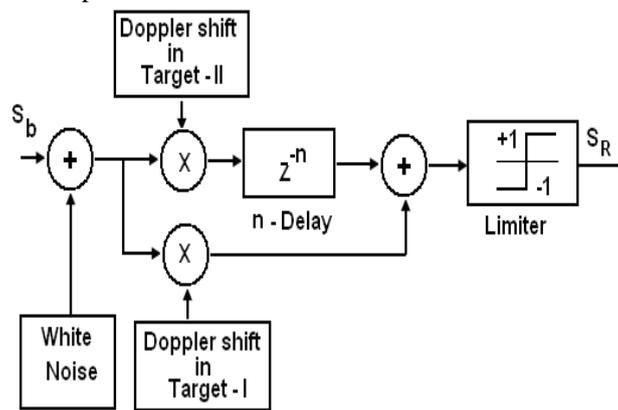
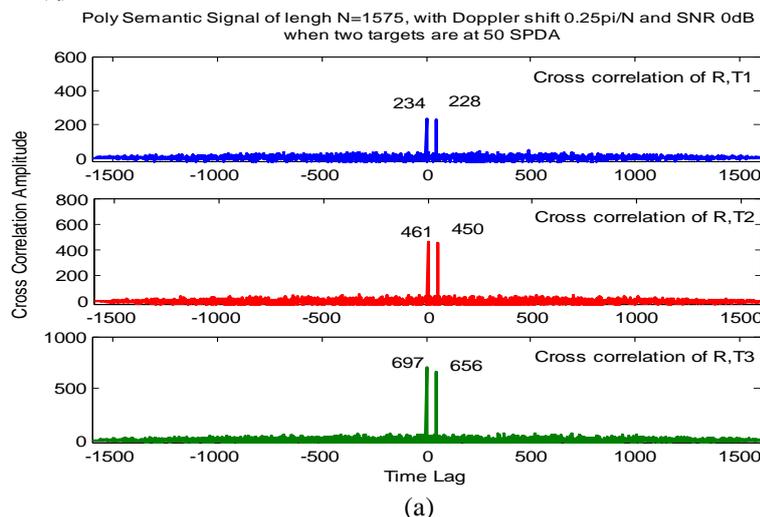


Fig. 8 Target Model When Two Targets are at n-SPDA.

Detection Performance

Let us consider a K_a -band 30 GHz radar, transmitting a poly-semantic sequence of length $N=1575$ with pulse interval of $78.75\mu s$. The sub-pulse time interval τ is 50 ns (signal bandwidth is 20 MHz and range resolution is 7.5 m). At the receiver, the resultant waveform is multiply interpreted for coincidence detection. For range resolution ability, consider a target model when a dispersed echo is reflected from two targets located at sub-pulse duration apart (SPDA) of zero to (N-1). Consider two targets moving with the same relative velocity in noisy environment. Fig. 9 shows the poly-semantic sequence of length 1575 when the two targets are separated by 50 SPDA with both Doppler shift = $0.25\pi/N$ at different values of (a) SNR (η) = 0 dB (b) SNR (η) = -5 dB (c) SNR (η) = -10 dB.



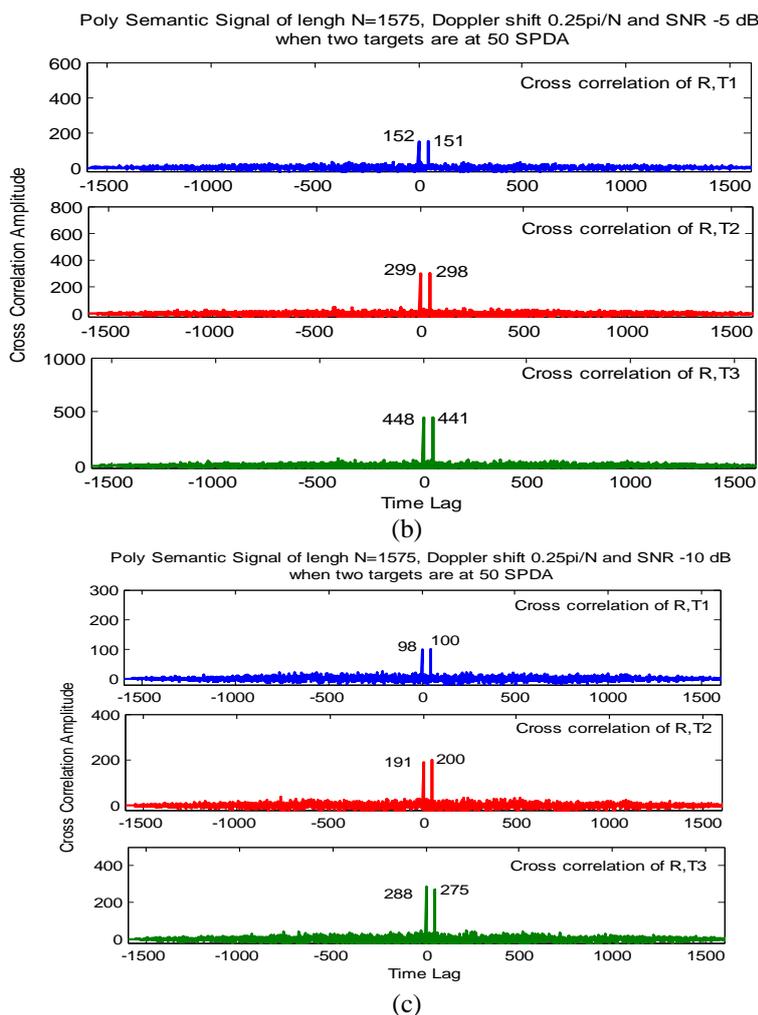


Fig. 9 Poly-Semantic Sequence of Length 1575 When The Two Targets are Separated by 50 SPDA With Doppler Shift = $0.25\pi/N$ at (A) SNR (η) = 0 dB (B) SNR (η) = - 5 dB (C) SNR (η) = -10 dB.

IV. CONCLUSION

In this paper poly-semantic sequences are analyzed for the detection of multiple targets in high density additive noise and Doppler environment for the application of high resolution Doppler radar system. Table I shows that the PSS have higher figure of merit than any other poly alphabetic sequence in noise free environments particularly at larger sequence lengths. These results provide the evidence that the PSS with larger pulse compression ratios can achieve the range side lobe level below 14.78 dB. This is significance improvement over conventional pulse compression sequences [13] and poly-phase alphabetic sequences [6] which provide side lobe level of 13.42 dB at length $N > 1638$ under noise free environment. This advantage arises because when the binary sequence is designed using 2nd order HBT algorithm, it performs recursive search such that the multiple interpretations of PSS of larger length reinforce each other through matched filtering and coincidence detection. The PSS has significant advantage of noise interference and Doppler tolerance with η below 20 dB at length $N > 4000$. Another important advantage of PSS is that their detection ability is further improved in noise free or noisy environment through coincidence detection scheme. The poly-semantic sequences at higher lengths with coincidence detection has noise tolerance of $\eta = -10\text{dB}$ with Doppler tolerance of $0.25\pi/N$. While compared with poly-phase sequences, a poly-semantic sequence has achieved better noise rejection ability, higher range resolution and superior Doppler tolerance. These examining results lead PSS to be very suitable for the high resolution Doppler radar systems. However, these advantages will be achieved with an additional affordable signal processing at the receiver.

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